

NORM BOUNDS ON THE SUM OF BLOCK DIAGONAL MATRICES

CHI-KWONG LI AND ROY MATHIAS

Abstract. We bound the norm of the sum of block diagonal matrices whose block structures may not be compatible, and use the result to bound the norm of banded positive semidefinite matrices. We consider the extension of the result to other norms.

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