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ON MAXIMAL FUNCTION AND FRACTIONAL INTEGRAL, ASSOCIATED WITH THE BESSEL DIFFERENTIAL OPERATOR

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Abstract. In this paper we consider the generalized shift operator, generated by Bessel differential operator B, by means of which maximal functions (B-maximal functions) and fractional integrals (B-fractional integrals) are investigated. The $L_p(B)$-boundedness result for the B-maximal function and $(L_p(B), L_q(B))$-boundedness result for the B-fractional integral are obtained.

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