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HADAMARD–TYPE INEQUALITIES FOR GENERALIZED CONVEX FUNCTIONS

MIHÁLY BESSENYEI AND ZSOLT PÁLES

Abstract. In this paper we investigate (ω_1, ω_2)-convex functions and obtain characterization theorems and Hadamard-type inequalities for them.

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