

STABILITY OF IMPLICIT RESOLVENT DYNAMICAL SYSTEMS

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Abstract. In this paper, we propose and analyze implicit resolvent dynamical systems associated with mixed quasi variational inequalities by using the techniques of the resolvent operators. We prove that the globally asymptotic stability of these dynamical systems requires monotonicity of the operator. We also discuss some special cases, which can be obtained from our main results.

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