

## ON KY FAN'S INEQUALITY AND ITS ADDITIVE ANALOGUES

J. ROOIN

*Abstract.* In this paper we give a discrete proof of Ky Fan's inequality. Also, we extend the additive analogues of Ky Fan's inequality to a very general case and give some applications.

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