A –STATISTICAL CONVERGENCE OF APPROXIMATING OPERATORS

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Abstract. In this paper we provide various approximation results concerning the classical Korovkin theorem via A-statistical convergence. We also study the rates of A-statistical convergence of approximating positive linear operators and give some examples.

Mathematics subject classification (2000): 41A25, 41A36; 40A05.
Key words and phrases: A-statistical convergence, sequence of positive linear operators, the Korovkin theorem.

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