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CONFORMAL BOUNDARY AND ALMOST OPEN BALLS

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Abstract. We establish a generalization to an inequality that can be used to measure how badly the intersection of an open ball of the euclidean space with the conformal boundary, i.e. the metric boundary of a conformal deformation of the unit ball $\mathbb{B}^n$, fails to be open in the euclidean sense. As an application to this, we show among other things that every point of a conformal boundary can be approached along a euclidean geodesical arc in a bounded set with respect to the intrinsic metric of conformal boundary.

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