Mathematical
Inequalities
& Applications
Volume 7, Number 3 (2004), 405–418

ON THE MAXIMUM PRINCIPLE FOR ELLIPTIC OPERATORS

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Abstract. In this paper we obtain some estimates for solutions of second order elliptic equations whose leading coefficients are functions of vanishing mean oscillation.

Mathematics subject classification (2000): 35J25, 35B50.
Key words and phrases: Elliptic equations, a priori bounds, discontinuous coefficients.

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Paper MIA-07-41