

A SIMPLE PROOF FOR SOME IMPORTANT PROPERTIES OF THE PROJECTION MAPPING

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Abstract. In this paper, we give a simple proof for an important property of projection mapping under general G -norm.

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