

INTEGRAL CHARACTERIZATIONS FOR STABILITY OF LINEAR SKEW-PRODUCT SEMIFLOWS

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Abstract. We give necessary and sufficient conditions for uniform exponential stability of linear skew-product semiflows. Using the theory of Banach function spaces we obtain integral characterizations for this concept. We extend a stability theorem obtained by Rolewicz for evolution families, at the general case of linear skew-product semiflows.

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