

COMMUTATORS OF IMAGINARY POWERS OF LAPLACE OPERATORS

SUNGGEUM HONG

Abstract. We obtain continuity properties of commutators generated by the imaginary powers of the Laplace operator and BMO functions on Hardy spaces and certain Hardy type spaces.

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