

STABILITY OF AN INCOMPLETE GAMMA-TYPE FUNCTIONAL EQUATION

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Abstract. We investigate the Hyers-Ulam-Rassias stability of an incomplete gamma-type functional equation

$$f(\phi_1(x_1), \dots, \phi_n(x_n), \psi_1(y_1), \dots, \psi_m(y_m)) \\ = \theta(x_1, \dots, x_n, y_1, \dots, y_m)f(x_1, \dots, x_n, y_1, \dots, y_m) + \lambda(x_1, \dots, x_n, y_1, \dots, y_m)$$

with a restricted domain. By this result we obtain the stability of the incomplete gamma functional equation

$$f(x+1, y) = xf(x, y) + e^{-y}(y)^x$$

with a restricted domain.

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