

INEQUALITIES FOR A SIMPLEX AND ANY POINT

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Abstract. By applying an analytic inequality and the polar moment of inertia inequality in E^n , we establish some inequalities for the volume, facet areas and distances between any point of E^n and vertices of an n -simplex

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