

ON THE STABILITY OF AN ALTERNATIVE FUNCTIONAL EQUATION

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Abstract. We deal with the stability of the alternative functional equation

$$f(x+y) + f(x) + f(y) \neq 0 \implies f(x+y) = f(x) + f(y).$$

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