

## AN INEQUALITY FOR MIXED LP-NORMS

## HARI BERCOVICI AND DIRK VAN GUCHT

Abstract. Consider a nonnegative measurable function f defined on  $\Omega_1 \times \Omega_2$ , where  $\Omega_j$  is a probability space with probability measure  $\mu_i$ . We prove the inequality

provided that  $1\leqslant p\leqslant 2$ . The inequality fails in general if p>2. It also fails if one of the measures  $\mu_j$  has total mass greater than one. Curiously however, the inequality is true for all  $p\in [1,\infty)$  if the measures  $\mu_j$  are counting measures. This last fact follows from a subadditivity result proved by G. A. Raggio for p-entropies. Our inequality also has a formulation in terms of p-entropies.

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