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NEW ITERATIVE APPROXIMATION FOR A SYSTEM OF GENERALIZED NONLINEAR VARIATIONAL INCLUSIONS WITH SET–VALUED MAPPINGS IN BANACH SPACES

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Abstract. In this paper, we introduce and study a new system of generalized nonlinear variational inclusions involving generalized m-accretive mappings. By using the resolvent operator technique for generalized m-accretive mapping due to Huang and Fang [10], we also prove the existence theorems of the solution and convergence theorems of the generalized Mann iterative procedures with mixed errors for this system of variational inclusions in q-uniformly smooth Banach spaces.

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