

## GENERALIZATION AND SHARPNESS OF FINSLER–HADWIGER’S INEQUALITY AND ITS APPLICATIONS

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*Abstract.* In this paper, the following generalization and sharpness of Finsler-Hadwiger’s inequality is established

$$\sum a^\lambda \geq 2^\lambda 3^{1-\frac{\lambda}{4}} F^{\frac{\lambda}{2}} + \sum |a-b|^\lambda + \sum_{n=1}^m |a_n - b_n|^\lambda.$$

As consequence, an exponential Finsler-Hadwiger type inequality for tetrahedron is derived.

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*Key words and phrases:* Finsler-Hadwiger’s inequality, Weitzenböck’s inequality, power means inequality, triangle, tetrahedron.

### REFERENCES

- [1] O. BOTTEMA, R. Z. DJORDJEVIĆ, R. R. JANIĆ, D. S. MITRINOVIĆ AND P. M. VASIĆ, *Geometric Inequalities*, Wolters-Noordhoff, Groningen, 1969.
- [2] D. S. MITRINOVIĆ, J. E. PEČARIĆ AND V. VOLENEC, *Recent Advances in Geometric Inequalities*, Kluwer Academic Publishers, Dordrecht, Netherlands, (1989), 104–106.
- [3] D. S. MITRINOVIĆ, J. E. PEČARIĆ, V. VOLENEC AND J. CHEN, *Addenda to the Monograph: Recent Advances in Geometric Inequalities(I)*, Journal of Ningbo University, **4**, (2) (1991), 80–81.
- [4] Z. SHAN, *Geometric Inequality in China*, Jiangsu Education Publishing House, Nanjing, (1996), 82–86 (in Chinese).
- [5] G. HARDY, J. E. LITTLEWOOD AND G. PÓLYA, *Inequalities*, 2nd ed. Cambridge University Press, Cambridge, UK, 1952.
- [6] S. H. WU, *Generalization of some inequalities for tetrahedron*, Journal of Longyan Teachers College, **21**, (3) (2003), 8–12 (in Chinese).