

SOME FRACTIONAL DIFFERENTIAL INEQUALITIES AND THEIR APPLICATIONS

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Abstract. We consider some inequalities involving derivatives of non-integer order. These inequalities arise naturally when investigating differential equations of fractional order. We find some bounds for solutions of these inequalities and give some applications.

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