

## SOME MAXIMUM PRINCIPLES FOR A CLASS OF ELLIPTIC BOUNDARY VALUE PROBLEMS

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*Abstract.* For a class of elliptic boundary value problems we construct, in this paper, some general elliptic inequalities from which we derive maximum principles and we also give some applications in physics and geometry of surfaces.

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