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THE STABILITY OF A WILSON TYPE AND A PEXIDER TYPE FUNCTIONAL EQUATION

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Abstract. In this paper we study the stability of the Wilson type functional equation $f(x+y)-f(x-y)=2g(x)g(y)$ and the Pexider type functional equation $f(x+y-xy)=(1-x)^{\alpha}g(y)+(1-y)^{\alpha}h(x)$, respectively.

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