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# HYERS–ULAM STABILITY OF FIRST ORDER LINEAR PARTIAL DIFFERENTIAL EQUATIONS WITH CONSTANT COEFFICIENTS

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*Abstract.* In this paper, we prove the Hyers-Ulam stability of first order linear partial differential equations with constant coefficients

$$au_x(x,y) + bu_y(x,y) + cu(x,y) + d = 0,$$

where $a, b \in \mathbb{R}$ and $c, d \in \mathbb{C}$ are constants with $\Re(c) \neq 0$ and $\Re(c)$ denotes the real part of $c$.

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