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OPTIMAL BOUNDS FOR LINEAR FUNCTIONALS ON MONOTONE FUNCTIONS

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Abstract. We determine optimal bounds on linear functionals over the space of square integrable functions on a finite interval, restricted to the nondecreasing elements of the subspace orthogonal to constants. We discuss conditions of bounds attainability and present exemplary applications.

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