

## GENERALIZED VECTOR QUASI-VARIATIONAL-LIKE INEQUALITIES

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*Abstract.* In this paper, some existence theorems for the generalized vector quasi-variational-like inequalities without monotonicity are obtained.

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*Key words and phrases:* set-valued mapping, generalized vector quasi-variational-like inequalities,  $L$ - $\eta$ -condition, existence.

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