Mathematical
Inequalities
& Applications
Volume 10, Number 3 (2007), 587–595

SOME TWO–SIDED BOUNDING INEQUALITIES FOR THE BUTZER–FLOCKE–HAUSS OMEGA FUNCTION

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Abstract. A new integral representation is obtained for the Butzer-Flocke-Hauss complete real-argument Omega function $\Omega(x)$, which is closely associated with the complex-index Bernoulli function $B_\alpha(z)$ and with the complex-index Euler function $E_\alpha(z)$. Three two-sided bounding inequalities are given for this Omega function and their efficiency is also discussed.

Mathematics subject classification (2000): 33E20, 33E30, 34A30, 34A40.
Key words and phrases: Butzer-Flocke-Hauss complete omega function, Chaplygin type differential inequality, Chaplygin type comparison theorem, Dirichlet series, integral representation of the Omega function, Laplace integral representation of Dirichlet series.

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Paper MIA-10-55