

SOME INEQUALITIES FOR UNIFORMLY LOCALLY UNIVALENT FUNCTIONS ON THE UNIT DISK

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Abstract. In this paper, we will consider some inequalities for a certain subclass $B(\lambda)$ of uniformly locally univalent holomorphic functions on the unit disk in terms of the norm of pre-Schwarzian derivative. We also investigate the relationships between the class $B(\lambda)$ and the Hardy space.

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