

## SOME NEW RETARDED VOLTERRA–FREDHOLM TYPE INTEGRAL INEQUALITIES WITH POWER NONLINEAR AND THEIR APPLICATIONS

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*Abstract.* Some new explicit bounds on solutions to a class of new nonlinear retarded Volterra-Fredholm type integral inequalities are established, which can be used as effective tools in the study of certain integral equations. Applications examples are also indicated.

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