

## AN EXPLICIT BOUND FOR THE ERROR TERM OF THE DEVELOPMENT AT $s = 1$ OF A SET OF LACUNARY SERIES

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*Abstract.* An explicit bound for the error term of the expansion of  $F_n(x) := \sum_{k=0}^{\infty} k^n x^{2^k}$  as  $x \rightarrow 1^-$  is given.

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