ON CONVEX FUNCTIONS OF HIGHER ORDER

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Abstract. Based on J. L. W. V. Jensen's concept of convex functions as well on its generalization by E. M. Wright and related to T. Popoviciu's convexity notions, higher-order convexity properties of real functions are introduced and surveyed.

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