APPROXIMATION BY A KANTOROVICH VARIANT OF
THE BLEIMANN, BUTZER AND HAHN OPERATORS

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Abstract. We study the approximation properties of a Kantorovich variant of the Bleimann, Butzer and Hahn operators for locally bounded functions, and estimate their rate of convergence by some techniques of probability theory and analysis methods.

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