

## COMPACTNESS OF INTEGRAL OPERATORS IN LEBESGUE SPACES WITH MIXED NORM

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*Abstract.* Compactness of certain double sized multidimensional integral operators is characterized in terms of the corresponding two-dimensional operators in the framework of weighted Lebesgue spaces with mixed norm.

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