

A CROSS-RATIO INEQUALITY FOR QUASICIRCLES

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Abstract. In this note we give a geometric characteristic for quasicircles by making use of cross-ratios, which is analogous to quadruple points identity of circles.

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