

ON SOME FURTHER SECOND ORDER INTEGRAL INEQUALITIES

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Abstract. Some weighted quadratic integral inequalities of the second order involving a function, its first and second derivative has been derived using the uniform method of obtaining integral inequalities. An example in which some new integral inequalities with Chebyshev weight functions appeared has been considered.

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