

COMPARISON THEOREM FOR TWO-PARAMETER MEANS

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Abstract. The comparison theorem for

$$R(u, v; r, s; x, y) = \left(\frac{E(r, s; x^v, y^v)}{E(r, s; x^u, y^u)} \right)^{1/(v-u)}, \quad u \neq v,$$

where E is the Stolarsky mean, is proved. This generalises the results of Leach, Sholander and Páles.

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