

AN EXTENSION OF THE LUPAŞ THEOREM FOR HERMITE–HADAMARD FUNCTIONALS

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Abstract. In this paper we investigate a representation theorem of Lupaş type for Hermite–Hadamard functionals. We use the obtained results by considering integral mean values with respect to certain signed measures.

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