

CONTINUITY PROPERTIES FOR RIESZ POTENTIALS OF FUNCTIONS IN MORREY SPACES OF VARIABLE EXPONENT

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Abstract. Our aim in this paper is to deal with continuity properties for Riesz potentials of functions in Morrey spaces of variable exponent. The modulus of continuity is determined by the structure of Morrey space.

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