

A SHARP OSTROWSKI-GRÜSS TYPE INEQUALITY

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Abstract. The main purpose of this paper is to use a variant of Grüss inequality to obtain a sharp Ostrowski-Grüss type inequality for absolutely continuous functions whose derivatives are bounded both above and below almost everywhere. Thus we provide improvement and generalization of some previous results.

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