

STRIPS AND HYPERBOLAS FOR ZEROS OF POLYNOMIALS IN TERMS OF THEIR HERMITE EXPANSION

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Abstract. We obtain estimates for strips and hyperbolas containing all the zeros of a polynomial given by its Hermite expansion, by combining some ideas of Turán and the classical methods of Fujiwara, Ballieu, Cowling and Thron.

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