

MULTIPLICATIVE PERTURBATION BOUNDS FOR WEIGHTED UNITARY POLAR FACTOR

HU YANG, HANYU LI AND HUA SHAO

Abstract. The multiplicative perturbation bounds for weighted unitary polar factor are considered in the weighted unitary invariant norm, weighted spectral norm, and weighted Frobenius norm in this paper. As the special cases, new bounds for subunitary and unitary polar factor are also derived. These new bounds improve the corresponding results published recently to some extent.

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