

THE SHARP SOBOLEV TRACE INEQUALITY IN A LIMITING CASE

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Abstract. A limiting case of the Sobolev trace inequalities is investigated and the best constant for the case is computed. Moreover, when $n = 1$, the same result is obtained from recognizing the Euler-Lagrange equation for the inequality as the mean curvature formula of plane curves.

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