CLOSED OPERATOR INEQUALITIES AND OPEN PROBLEMS

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Abstract. In [3, 4], we have given some characterizations of some subclasses of complex Hilbert space normal operators by inequalities. In this note, we shall reformulate these results using a concept of closed inequalities. Also, we shall give some new characterizations. Some open problems concerning closed inequalities are posed at the end of this note.

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