

IMPROVED HARDY–SOBOLEV INEQUALITIES FOR RADIAL DERIVATIVE

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Abstract. We prove some Hardy-Sobolev inequalities for radial derivative and obtain the corresponding sharp constant.

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