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VOLTERRA COMPOSITION OPERATORS FROM WEIGHTED–TYPE SPACES TO BLOCH–TYPE SPACES AND MIXED NORM SPACES

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Abstract. The boundedness and compactness of the Volterra composition operator from a class of weighted-type spaces to Bloch-type spaces and mixed norm spaces on the unit ball are completely characterized in this paper.

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