INEQUALITIES AND MAJORISATIONS FOR THE
RIEMANN–STIELTJES INTEGRAL ON TIME SCALES

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Abstract. We prove dynamic inequalities of majorisation type for functions on time scales. The results are obtained using the notion of Riemann–Stieltjes delta integral and give a generalization of [App. Math. Let., **22**, 3 (2009), 416–421] to time scales.
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