MULTIPLICATIVE SOBOLEV INEQUALITIES
OF THE LADYZHENSKAYA TYPE

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Abstract. We present a set of multiplicative Sobolev inequalities that yield less restrictive embedding and Trudinger-type results. The proofs are elementary and deduced only from a multiplicative inequality of Gagliardo-Nirenberg and Hölder's inequality with no recourse to any potential estimates.

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