

MONOTONICITY OF FUNCTIONS INVOLVING Q-GAMMA FUNCTIONS

CHRYSI G. KOKOLOGIANNAKI

Abstract. We give monotonicity properties of some functions involving q-Gamma functions. The results are q-analogue of results concerning Gamma function and generalize some known results.

Mathematics subject classification (2010): 33B15, 33D05, 26D07, 24A48.

Keywords and phrases: q-Gamma function, monotonicity properties, inequalities.

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