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# CHEBYSHEV TYPE INEQUALITIES FOR SYNCHRONOUS VECTORS IN BANACH SPACES

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*Abstract.* In [3] Chebyshev type inequalities are proved for separable finite sequences. In this paper, the applicability of that notion is extended and replaced by a relation of synchronicity. In consequence, new sufficient conditions for Chebyshev type inequalities are derived.

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