WEYL TYPE THEOREMS AND CLASS $A(s,t)$ OPERATORS

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Abstract. In this note we show that if T belongs to the class $A(s,t)$ for some $0 < s,t \leqslant 1$ then Weyl's and generalized Weyl's theorems hold for $f(T)$ for every analytic function f on some open neighborhood of $\sigma(T)$. We also show that operators in $A(s,t)$ satisfy the Bishop's property (β).

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