

MEANS INVOLVING LINEAR FUNCTIONALS AND n -CONVEX FUNCTIONS

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Abstract. In this article we study Cauchy type means for linear functionals. We examine their monotonicity properties, and even more we give new type of inequalities after we proved exponential convexity. We cover a number of well-known means such as generalized Stolarsky, Stolarsky-Tobey and Whiteley means.

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