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GROTHENDIECK'S INEQUALITY AND APPLICATIONS

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Abstract. We give a small survey in connection with the famous Grothendieck's inequality. We consider some classical applications, an application to the geometry of Banach spaces as well as applications to the well known problem of whether the S_p-algebras with their Schur products should be Q-algebras.

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