

A REFINEMENT OF THE DISCRETE JENSEN'S INEQUALITY

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Abstract. We give a refinement of the discrete Jensen's inequality in the convex and mid-convex cases. For mid-convex functions our result is a common generalization of known inequalities. We illustrate the scope of the results by applying them to some special situations.

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